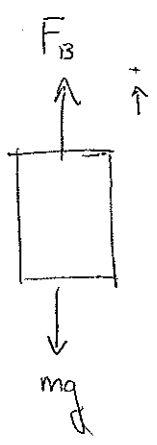
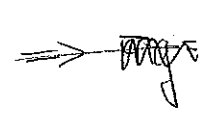


3 A)



$$\sum F_y = F_B - mg = 0 \quad m(0)$$

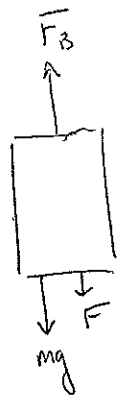


$$(1000 \text{ kg/m}^3) (0.04 \text{ m}^2) (0.6 \text{ m}) (10 \text{ m/s}^2) = 240 \text{ N}$$

$$\Rightarrow mg = F_B = \rho_w V_w g = \rho_w (A) (h)$$

↳ since the buoyancy force is the weight of the displaced water.

B)



$$\sum F_y = F_B - mg - F = m(0)$$

$$\Rightarrow F = F_B - mg = (1000 \text{ kg/m}^3) (0.04 \text{ m}^2) (0.7 \text{ m}) (10 \text{ m/s}^2) - 240 \text{ N} = 40 \text{ N down!}$$

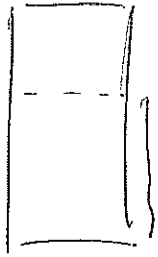
c) Once again:

$$\sum F_y = F_B - mg - F = m(0)$$

$$\Rightarrow F = F_B - mg = (1000 \text{ kg/m}^3) (0.04 \text{ m}^2) (0.8 \text{ m}) (10 \text{ m/s}^2) - 240 \text{ N} = 80 \text{ N}$$

So we need 40N in addition to part B. This seems linear to me!

D) Let's take a look at the buoyancy force as a function of how much is submerged.



$$F_B = (1000 \text{ kg/m}^3)(0.04 \text{ m}^2)(10 \text{ m/s}^2)h = \underbrace{(400 \text{ N/k})}_k h$$

↳ identify this as k

$$\omega = \sqrt{k/m} = \sqrt{\frac{400 \text{ N/m}}{24 \text{ kg}}} = \boxed{4.08 \text{ rad/sec}}$$

E) For a damped oscillator, the equation is:

$$y(t) = A e^{-bt/2m} \cos(\omega t - \phi), \quad A = -2 \text{ cm}$$

but since it starts from rest, $\phi = 0$, so we're left with:

$$y(t) = A e^{-bt/2m} \cos(\omega t)$$

Now, at the top of the cycle, $t = \frac{T}{2} = \frac{2\pi}{2\omega} = \boxed{\frac{\pi}{\omega}}$

$$y\left(\frac{\pi}{\omega}\right) = A \left(e^{-b\pi/2m\omega} \right) \left(\cos\left(\frac{\pi}{\omega}\omega\right) \right) = \textcircled{0} - A e^{-b\pi/2m\omega} = \textcircled{0} \text{ cm} = 1.8 \text{ cm}$$

$$\Rightarrow e^{-b\pi/2m\omega} = \frac{-1.8 \text{ cm}}{A} = 0.9$$

$$\Rightarrow \frac{-b\pi}{2m\omega} = \ln(0.9) = -0.1054$$

$$\Rightarrow b = \frac{(0.1054)(2m\omega)}{\pi} = \frac{(0.1054)(2)(24 \text{ kg})(4.08 \text{ Hz})}{\pi} = \boxed{6.57 \text{ kg/sec}}$$